## AN IMPORTANT NOTE ABOUT ACCURACY IN CALCULATIONS

CASA expect extreme accuracy in all calculations and take-off or landing charts. The level of accuracy required is far beyond what would be considered acceptable in the 'real world'.

When performing multi-step calculations, you should keep all intermediate decimal places on your calculator and then round the final answer to the nearest appropriate whole number.

What do I mean by appropriate whole number? Glad you asked that one.
For minimum fuel or ballast required calculations, round $\boldsymbol{u} \boldsymbol{p}$ to the next whole number. If there is any decimal place in the final answer, the answer should be rounded up.
So 167.1745 gallons should be rounded up to 168 gallons.
For maximum weight limitations calculations round down to the next whole number. If there is any decimal place in the final answer, the answer should be rounded down. So 167.8745 kg should be rounded down to 167 kg .

Otherwise, if the first decimal place in the final answer is 5 or more, the answer should be rounded up. So 167.5475 should be rounded up to 168 and if the first decimal place is less than 5 , the answer should be rounded down. So 167.4475 is rounded down to 167 .

The examiner will make it clear as to which way the final answer is to be rounded.
Since CASA does not disclose how much margin of error is allowed for people who choose to do multiplication or division on a flight computer e.g for PNR, ETP or time, speed and distance calculations, it is strongly recommended that you use an electronic calculator for all operations except for flight planning headings and ground speeds and conversions between CAS and TAS.

Also, extreme care must be taken when using any take-off or landing performance chart. Make sure that you have a sharp pencil (and invest in a pencil sharpener). Make sure that all horizontal and vertical lines are precise. Take great care in interpolation between published values. Very little deviation is permitted from CASA's 'perfect answer'.

## Calculations in this book have been presented as follows.

## Single step calculations

The answer is taken to the nearest appropriate whole number.

## Multi-step calculations

Intermediate calculations are taken carry at least one decimal place with the final answer shown to the nearest appropriate whole number.

## THE EQUI-TIME POINT [ETP] also called CRITICAL POINT - [CP]

The Equi - Time Point [ETP] is also sometimes called the Critical Point [CP]. It is simply the point along a given route segment from which it will take the same time to go on, or return to the starting point. This point would be of interest to pilots who are planning a flight which involves a long segment over desolate country with no suitable aerodromes en-route where a landing could be made in the event of an emergency, a long segment over water, or an IFR or NGT VFR flight with no en-route aerodromes equipped with appropriate navigation aids or lighting. Once the ETP has been calculated, it becomes one of the factors that must be considered in an emergency. If an emergency arises before the ETP has been reached, it will be faster to go back to the departure point. If an emergency arises after the ETP has been passed, it will be faster to continue to the destination.

Obviously, if there was no head or tail wind component along track, the ETP would be half way.

Fig 4.26
No wind


In the example illustrated in Fig 4.26 above, for an aircraft with a TAS of 180 kt , the ETP would be half way between A and B in no wind. It would take the same time to fly from the ETP to A as it would to fly from the ETP to B.

If we now consider wind component of 20 kt blowing from B to A , what will happen to the ETP?
Fig 4.27


If we continue towards B , the ground speed will be 160 kt , if we return to A , the ground speed will be 200 kt . It follows that the ETP must be closer to B since the time taken to fly from the ETP to B at 160 kt must equal the time taken to fly from the ETP to A at 200 kt [fig 4.27].

THE ETP [also called CP] WILL ALWAYS BE HALF WAY IN NO WIND.

IF A WIND EXISTS, THE ETP WILL ALWAYS MOVE UP-WIND FROM HALF WAY.

## The ETP calculation.

To continue with this example, let's assume that the total distance from A to B is 350 nm . To calculate the actual position of the ETP between $A$ and $B$ we need to know three things.

1. The ground speed we expect if we choose to continue on to B [GS on]
2. The ground speed we expect if we choose to return to A [GS home]
3. The total distance between A and B

In this example,

| GS on | $=160 \mathrm{kt}$ |
| :--- | :--- |
| GS home | $=200 \mathrm{kt}$ |
| Total distance | $=350 \mathrm{~nm}$ |

The ETP formula is,

$$
\begin{aligned}
\text { Distance to ETP } & =\frac{\text { Total distance } \mathbf{x} \text { GS home }}{\text { GS home }+ \text { GS on }} \\
& =\frac{350 \times 200}{200+160} \\
& =\frac{70000}{360} \\
& =194 \mathrm{~nm} \text { from A }
\end{aligned}
$$

Fig 4.28


Proof:
The time to fly from the ETP to B is $155.6 \mathrm{~nm} @ 160 \mathrm{kt}=58.3 \mathrm{~min}$
The time to fly from the ETP to $A$ is 194.4 nm @ $200 \mathrm{kt}=58.3 \mathrm{~min}$
Note that even though the examination does not require it, you can always prove that the ETP you have calculated is correct. I think it is a good idea to do this in the first few exercises that you try to ensure that you are not just blindly using a formula, but that you understand what the answer means.

Computer solution:


Fig 4.29 To solve the ETP calculation on your computer, simply place the sum of the ground speeds on the inside scale beneath the total distance on the outside [Fig 4.29].

The distance to the ETP is read against the GS home on the inside scale. Note also that when the wind is given as $\boldsymbol{a}$ headwind component directly along the flight planned track, the GS on is actually TAS minus the wind, and the GS home is the TAS plus the wind,

$$
\begin{aligned}
\text { GS on }+ \text { GS home } & =[\text { TAS }- \text { wind }]+[\text { TAS }+ \text { wind }] \\
& =2 \times \mathrm{TAS}
\end{aligned}
$$

A simplified version of the ETP formula when the wind is given as a head or tailwind component directly along the flight planned track becomes-

## Distance to ETP

Total distance x GS home
$=\frac{2 \times T A S}{}$
However, if the wind is given as a velocity instead of a component, you will need to calculate the two ground speeds on your flight computer.

## SINGLE ENGINE ETP FOR MULTI-ENGINE AEROPLANES.

If you do a multi-engine endorsement, you will need to know how to calculate a ETP which assumes that, in the event of an engine failure en-route, the aircraft will be flown either on to B on the one remaining engine, or back to A on the one remaining engine.
To calculate this point we simply use the same formula except that the TAS we consider is the single engine TAS. Assuming the aircraft we have been considering has a single engine TAS of 110 kt , the distance to the single engine ETP is [See Fig 4.30]:

Fig 4.30
Dist to
SE ETP $=$
$\frac{\text { Total distance } \times \text { SE GS home }}{2 \times \text { SE TAS }}=\frac{350 \times 130}{220}=206.8 \mathrm{~nm}$ from A
Proof:


Time to fly from the ETP to B on one engine is 143.2 nm @ 90 kt
$=\quad 95.4 \mathrm{~min}$
Time to fly from the ETP to A on one engine is 206.8 nm @ 130 kt
$=\quad 95.4 \mathrm{~min}$

## Deriving the ETP formula from basic principles.

For those of you with a love of maths, here is the derivation of the ETP formula [Fig 4.31]. This is not required knowledge for the examination.


Let $\mathrm{D}=$ total distance
Let $\mathrm{d}=$ distance to ETP
Let $\mathrm{H}=\mathrm{GS}$ home
Let $\mathrm{O}=\mathrm{GS}$ on

If the times are to be equal,

$$
\begin{aligned}
& \frac{\mathrm{d}}{\mathrm{H}}=\frac{\mathrm{D}-\mathrm{d}}{\mathrm{O}} \\
& \text { so } \quad \frac{d}{H}=\frac{D}{O}-\frac{d}{O} \\
& \text { and } \frac{\mathrm{d}}{\mathrm{H}}+\frac{\mathrm{d}}{\mathrm{O}} \quad=\frac{\mathrm{D}}{\mathrm{O}} \\
& { }^{\mathrm{d}}\left(\frac{1}{\mathrm{H}}+\frac{1}{\mathrm{O}}\right)=\frac{\mathrm{D}}{\mathrm{O}} \\
& { }_{\mathrm{d}}\left(\frac{\mathrm{HO}}{\mathrm{H}}+\frac{\mathrm{HO}}{\mathrm{O}}\right)=\frac{\mathrm{D} x}{\mathrm{O}} \mathrm{HO} \quad \text { [Multiplying both sides by HO] } \\
& \mathrm{d}[\mathrm{O}+\mathrm{H}] \quad=\mathrm{DxH} \\
& \text { and } d=\frac{D \times H}{O+H}
\end{aligned}
$$

Before we go further, make sure you are familiar with the flight computer solutions for flight planning heading and ground speed for a given TAS, wind and flight planned track.

Here is an example.

Flight Planned Track
Forecast wind from
Magnetic variation True Air Speed
$040^{\circ} \mathrm{M}$
$120^{\circ} \mathrm{T}$ at 20 kt
$10^{\circ} \mathrm{E}$
180kt

Consider this example. You are to fly outbound on the $040^{\circ} \mathrm{M}$ track and then turn around and fly back home on the reciprocal track of $220^{\circ} \mathrm{M}$. Find the ground speed to expect outbound and also on the return trip (we are not interested in the heading in this example). The wind is given as a velocity, not a head or tail wind component, so you must calculate the ground speeds on your flight computer.


Now consider an extreme example. A strong wind is at exactly $90^{\circ}$ to the flight planned track. A common misconception is that, if the wind is at $90^{\circ}$ to the track, there would be no head or tailwind component and the ground speed would be the same as the TAS.


This is not the case however, because when the wind is at $90^{\circ}$ to the track, it is necessary to fly into wind to counter the drift.

So there will be a headwind component and the ground speed will actually be less than the TAS.

Here is an example of a strong wind at right angles to track

| Flight Planned Track | $330^{\circ} \mathrm{M}$ |
| :--- | :--- |
| Forecast wind from | $250^{\circ} \mathrm{T}$ at 40 kt |
| Magnetic variation | $10^{\circ} \mathrm{E}$ |
| True Air Speed | 150 kt |

You are to fly outbound on the $330^{\circ} \mathrm{M}$ track and then turn around and fly back home on the reciprocal track of $150^{\circ} \mathrm{M}$. Find the ground speed to expect outbound and also on the return trip (we are not interested in the heading in this example).


With the wind at right angles to track some might reason that, since there is no head or tail wind component acting along the track, the ground speed should be the same as the TAS. As we have seen that is not true. In this example, the ground speed is 5 knots less than the TAS (145kt). That is because the heading is $15^{\circ}$ further into wind than the track so the aircraft must fly into wind to allow it to remain on track.


## 3

Find $15^{\circ}$ on the effective TAS window and read the corresponding effective TAS (145). Add or subtract the head or tail wind component to or from the effective TAS to find the ground speed.

There is no head or tail wind component on the FPT, so 145 kt is also the ground speed.

## 2

The crosswind component is 40 kt . So find 40 kt on the outside scale and convert it into a drift angle $\left(15^{\circ}\right)$. If the drift is greater than $10^{\circ}$ you need to find effective TAS (See 3).

As we cover equi-time point and point of no return calculations in this chapter, we will often need to calculate the ground speed to expect on the outbound leg of a flight as well as the ground speed to expect if we decide to return to out starting point. Sometimes we will need to add those two ground speeds together.

Of course if there is no wind at all, the ground speed will be the same as the TAS in both directions. However, if a wind is introduced, we will have to consider the effect it will have on the ground speed.

There are two ways that an examiner can describe the wind. It can be given as a headwind or tailwind component on track. In that case we simply apply the wind component to the TAS to obtain the ground speeds. Add the wind component to the TAS if it is a tailwind and subtract the wind component from the TAS if it is a headwind.

For example, for a TAS of 180 kt and a 20 kt headwind component, the ground speed outbound would be 180-20 $=160 \mathrm{kt}$, while the ground speed on the return leg would be $180+20=200 \mathrm{kt}$


In this case, if you added the two ground speeds you would get-
Ground speed out = TAS - wind component
Ground speed home $\quad=$ TAS + wind component
Sum of the ground speeds $=$ TAS + wind component + TAS - wind component
$=2 \times$ TAS (the two wind components cancel out)
However, if the wind is given as a velocity (direction and speed) in a direction other than directly along the track, the sum of the ground speeds will not be the same as $2 \times$ TAS. In that case, you will need to calculate the ground speeds on a flight computer as shown previously. This is especially important when the wind is strong and at a large angle to track.

In the example worked on the previous page, the ground speed out is 145 kt and the ground speed home is also 145 kt so the sum of the ground speeds is 290 kt whereas 2 x TAS is 300 kt . That's enough to give you an incorrect answer in an exam.

## So remember:

If the wind is given as a headwind or tailwind component along track, the sum of the ground speeds will simply be $2 x$ TAS.

If the wind is given as a velocity (direction and speed) at an angle to track, you must calculate the two ground speeds on a flight computer and then find their sum.

## AN EXAMPLE OF A SINGLE-ENGINE CRITICAL POINT CALCULATION.

An aeroplane is planning a flight from A to B . The flight planned track is $128^{\circ} \mathrm{M}$ and the distance $A$ to $B$ is 435 nm . The normal two engine cruising TAS is 150 kt . If the single engine TAS is 80 kt . The GAF indicates that a wind of 45 kt from $200^{\circ} \mathrm{T}$ is expected on the flight planned track at all levels. If the magnetic variation is $8^{\circ} \mathrm{E}$, find the distance from A to the single engine ETP [ignore climbs and descents].

The wind is given as a vector, so you must calculate the single engine ground speed out and home
Find the single engine ground speed out (also called ground speed on).


Find the single engine ground speed back (also called ground speed home).



Wind 192M @ 45kt. TAS 80kt. Crosswind 40. tailwind 20. Drift angle $30^{\circ}$. Effective TAS 69 plus the tailwind 89 kt Single engine ground speed home $=89 \mathrm{kt}$.

## SOLUTION.

Single engine GS on is
Single engine GS home is
Total distance
Distance to single engine critical point $=435 \times 89 \div 139=278.5 \mathrm{~nm}(279 \mathrm{~nm})$

Now that we know where the critical point is, how will we know when we have arrived there? If good visual features are not available, one of the most useful indicators would be the time it should take to get there. After you have calculated the ETP, you may often want to know the time it will take get to that point.

If we return to the example above, and assume that the flight planned TAS for normal two engine cruise was 150 kt , then the flight planned GS from A to B would be.


Track $128^{\circ} \mathrm{M}$
Wind from $192^{\circ} \mathrm{M}$ at 45 kt
TAS 150kt
Ground speed 125 kt (under grommet)
Ground speed out at normal cruise TAS

$$
=125 \mathrm{kt}
$$

Time to the ETP at normal cruise on 2 engines

$$
\begin{aligned}
& =279 \mathrm{~nm} @ 125 \mathrm{kt} \\
& =133.9(134 \mathrm{~min})
\end{aligned}
$$

## SOME IMPORTANT POINTS TO CONSIDER FOR MULTI-ENGINE AEROPLANES.

In the event of an engine failure before that time, we know it would be faster to go back. In the event of an engine failure after that time, it would be faster to continue on to B.
Note that the ETP simply tells us whether it would be faster to go on or to go home. However the fastest option may not necessarily be the safest option!

I suggest you read carefully CAO 20.6.3.2
Consider an IFR flight which has just passed through an area of thunderstorm activity with associated severe turbulence and icing. If an engine failed and the ETP had not been reached, it would be faster to go back - but you would have to be crazy to try it!

Don't forget that the altitude you can expect to maintain on one engine is likely to be much lower than your original planned cruise altitude [typically about 5000ft density height for most light twins]. Even though the ETP calculation may indicate that it is faster to go on after an engine failure, there is not much use trying if you can't maintain terrain clearance.

As is so often the case in aviation, there are many factors that must be considered - the ETP is just one of them.

Fig 4.32


## GOING BACK ?

Fig 4.32a


## GOING ON ?

Then there was the young pilot who was flying a Chieftain from a major airport to a country homestead. The weather was fine and beaut and there were no terrain problems on the short flight. When the left engine failed, the pilot decided that, since he had passed the single engine ETP, the best thing to do was to continue on to the ALA, where he successfully landed. The phone call to his boss went something like this.

Pilot: $\quad$ II had the engine failure, and since I had already passed the critical point, I continued on to land out here.

Boss: $\quad$ I've got news for you buddy, you've just passed a critical point in your career- you're fired!"

## CALCULATING THE POINT OF NO RETURN. [PNR]

The PNR is the maximum distance an aircraft can proceed in a given direction from its take off point before it becomes impossible for it to return with all reserves intact. It is obvious then that if all other factors remain constant, the distance to the PNR is governed by the amount of fuel on board at start up.

The first step in finding the PNR is to calculate the time that the aircraft can fly without using its fuel reserves. This time, expressed in minutes, is called the safe endurance.

## FINDING THE SAFE ENDURANCE

Let's investigate the safe endurance available for an aircraft on a CHTR flight if start up is with 180 gal , fuel flow is 28 gph , and the allowance for taxi and fixed reserve is 3 gal and 15 gal respectively.

| Total fuel at start up | $=180 \mathrm{gal}$ |
| :--- | :--- |
| Less start up and taxi allowance | $=3 \mathrm{gal}$ |
| Less fixed reserve | $=15 \mathrm{gal}$ |
|  | $=162 \mathrm{gal}$ |
| 162 gal is $110 \%$ of the trip fuel |  |
| available so $100 \%$ of the trip fuel | $=147.3 \mathrm{gal}$ |
| Fuel flow | $=28 \mathrm{gph}$ |
| $147 \mathrm{gal} @ 28 \mathrm{gph}$ |  |
|  | $=315.6 \mathrm{~min}$ |
| Safe endurance | $=316 \mathrm{~min}$ |

## TO FIND THE SAFE ENDURANCE :

1. FIND THE Trip fuel AVAILABLE.
2. CONVERT THE Trip fuel TO MINUTES AT CRUISE RATE.

In the CPL examination all questions on PNRs are based on normal two engine operations both out and back. Engine failure is not considered in the PNR calculation. Also a flight that has flown to its PNR and is returning to base is not considered as an emergency. Such a flight would be expected to have all the fuel reserves, including holding due weather, required by the operator and/or the CASA. No special consideration or priority would be given to the issue of airways clearances or traffic sequences.

Considering the example for the aircraft given above, the flight to the PNR and back to base must not be any longer than 315 mins .

Fig 4.33


## THE EFFECT OF WIND.

Continuing with this example, if there is no wind, the ground speed out to the PNR will be the same as the ground speed home. It follows that since the flight out and back must be 316 mins, the time to the PNR must be half of 316 [158] min. If there is no wind, the aircraft can fly out until half of its safe endurance is used - it must then return to base.

What happens if we introduce a wind? Now here's a chance to win some bets in the aero club bar! [See Fig 4.34 \& 4.35].

Consider this example,
Fig 4.33a


The distance from A to B is 100 nm . If an aircraft with a TAS of 100 kt flies from A to B, then turns around and flies back to A, how long will it take if there is no wind? [for simplicity ignore climbs, descents and the turn around].

$$
\begin{array}{ll}
\text { Time out is } 100 \mathrm{~nm} @ 100 \mathrm{kt} \text { GS } & =1 \text { hour } \\
\text { Time home is } 100 \mathrm{~nm} @ 100 \mathrm{kt} \mathrm{GS} & \\
\text { Total time out and back } & =2 \text { hours }
\end{array}
$$

Now, let's repeat the exercise with a 30 kt wind blowing from B towards A . Wouldn't you reckon that with a 30 headwind out and a 30 tailwind home, the wind effect should cancel out leaving a total flight time once again of 2 hours? Let's see what happens.
Fig 4.34


Where did the extra 12 min come from?

The answer is in the time spent in the headwind and the tailwind. The aircraft suffered the 30 kt headwind for 86 min , but it enjoyed the 30 kt tail wind for only 46 min . The winds don't cancel out because the headwind was acting for a longer time.

What if the wind was blowing from the other direction?

Fig 4.35


It doesn't matter whether the wind is a headwind or a tailwind, any wind at all will add to the time taken to complete the flight compared to the nil wind situation.

The PNR therefore, will always be at the greatest distance out in no wind. Any wind, head or tail, will reduce the distance to the PNR.

By the way, this will be true of any flight that returns to the starting point without landing. A typical navigation training flight that goes from A to B to C etc and back to A , will always take longer on a windy day than on a calm day no matter which direction the wind is coming from.

## CALCULATING THE TIME TO THE PNR.

Consider the following example:
A charter aircraft cruises at a TAS of 185 kt , and has a fuel flow during cruise of 28 gph . The tailwind component on the flight planned track is 25 kt and start up is with 120 gal . If 3 gal is allowed for start-up and taxi, and 15 gal is allowed for the fixed reserve, find the time to the PNR [ignore climb and descent].

STEP ONE: Find the safe endurance.

$$
\begin{array}{ll}
\text { Trip fuel available } & =[120-3-15] \div 1.1 \\
& =92.7 \mathrm{gal} \\
& =198.6 \mathrm{~min} \\
\text { At } 28 \mathrm{gph} & \text { Safe endurance }
\end{array}
$$

Fig 4.36


To calculate the time to the PNR you need to know:

1. Safe endurance
2. The GS home
3. The TAS

The formula is:
$\begin{aligned} \text { Time to PNR } & =\frac{\text { Safe endurance } \mathrm{x} \text { GS home }}{\text { SUM OF THE GSs (the wind was given as a component so use } 2 \times \text { TAS) }} \\ & =\frac{199 \times 160}{370} \\ & =86.1 \mathrm{~min}(86 \mathrm{~min})\end{aligned}$
If you fly out for more than 86 min you will not be able to return to A with all reserves intact.
DISTANCE TO THE PNR.
How far from A is the PNR?

For the 86 min spent flying out to the PNR you will be covering the ground at 210 kt . The distance to the PNR is

210 kt for $86.1 \mathrm{~min}=\mathbf{3 0 1} \mathbf{n m}$.

## PROOF:

The 301 nm flight out to the PNR will take 86 min [from the formula above].
The 301 nm flight back to $A$ will take 113 min [301nm @ 160 kt ].
The flight out to the PNR and back will take $113+86=199 \mathrm{~min}$.
This agrees with the safe endurance in STEP ONE.

## ANOTHER EXAMPLE

## AIRCRAFT DATA AND COMPANY POLICY

| NORMAL TAS | 190 kt |
| :--- | :--- |
| ASYMMETRIC TAS | 110 kt |
| NORMAL FUEL FLOW | $120 \mathrm{l} / \mathrm{hr}$ |
| ASYMMETRIC FUEL FLOW | 85 l hr |
| FUEL TANK CAPACITY | 680 l |
| FIXED RESERVE CALCULATED AT CRUISE RATE |  |
| VARIABLE RESERVE OF 10\% OF THE Trip fuel |  |
| START UP AND TAXI ALLOWANCE | 15 l |

Find the distance to the PNR on a charter flight for the aircraft whose data is shown above, if start up is with full tanks, a 20 kt head win component exists at all levels, and the departure aerodrome requires 60 min holding fuel [For company policy on fuel reserves, see question data above].

Fig 4.37

TAS $=190 \mathrm{kt}$ GS out $=170 \mathrm{kt}$.


Step 1:
Find the safe endurance.
Trip fuel available at start up $\quad=[$ Total fuel - taxi - fixed reserve - holding $] \div 1.1$
$=[680-15-90-120] \div 1.1$
$=413.6$ lts
@ 120 lts/hr
$=206.8 \mathrm{~min}$

## Step 2:

Find the time to the PNR
[ Note the PNR calculation assumes normal ops]

$$
\begin{aligned}
= & \frac{\text { Safe Endurance } \mathrm{x} \text { GS Home }}{2 \times \text { TAS (the wind was given as a component) }} \\
& \frac{206.8 \times 210}{380} \\
= & 114.3(114 \mathrm{~min})
\end{aligned}
$$

## Step 3:

Find the distance to the PNR

$$
\begin{aligned}
& =114.3 \text { min @ GS Out } \\
& =114.3 \mathrm{~min} @ 170 \mathrm{kt} \\
& =323.9 \mathrm{~nm} .
\end{aligned}
$$

Distance to the PNR is $\mathbf{3 2 4} \mathbf{n m}$.

## Revision exercises on ETP and PNR. [Answers on Page 134]

Aircraft data for use in Questions 1 to 11 of the following questions. The data below relate to a charter flight in a light twin-engine aeroplane.

Cruise TAS normal operation [two engines operating]
Normal fuel consumption [two engines operating]
Asymmetric cruising TAS [one engine operating]
Asymmetric fuel consumption [one engine operating]
Fuel consumption for holding if required
Start-up and taxi allowance

160 kt.
23 gallons/hr.
110 kt.
25 gallons/hr.
17 gallons/hr.
3 gallons.

Fuel reserves are in accordance with the CAAP [Calculate fixed reserve at cruise rate].

## Question No 1

You are planning a flight of 240 nm in the above aircraft. The flight planned track is $350^{\circ} \mathrm{M}$ and the wind is from $350^{\circ} \mathrm{M}$ at 40 kt . Find the distance and time to the ETP based on normal operation.
[a] The ETP is 90 nm and 45 minutes from the departure aerodrome
[b] The ETP is 150 nm and 45 minutes from the departure aerodrome
[c] The ETP is 90 nm and 27 minutes from the departure aerodrome
[d] The ETP is 150 nm and 75 minutes from the departure aerodrome

## Question No 2

FTP is $325^{\circ} \mathrm{M}$ and the wind is from $270^{\circ} \mathrm{T}$ at 30 kt . The variation is $10^{\circ} \mathrm{E}$. Using the data given, determine the distance to the PNR if the trip fuel available at take-off is 67 gallons.
[a] 312 nm
[b] 228 nm
[c] $\quad 190 \mathrm{~nm}$
[d] 160 nm

## Question No 3

The distance A to B is 300 nm , the FPT is $125^{\circ} \mathrm{M}$, wind is $330^{\circ} \mathrm{T}$ at 25 knots and variation is $12^{\circ} \mathrm{E}$, determine the distance and time required to fly from the ETP back to the departure aerodrome.
[a] The distance and time to return from the ETP is 128 nm and 56 mins
[b] The distance and time to return from the ETP is 128 nm and 36 mins
[c] The distance and time to return from the ETP is 178 nm and 56 mins
[d] The distance and time to return from the ETP is 56 nm and 178 mins .

## Question No 4

FPT A to B is $025^{\circ} \mathrm{M}$ : Wind $190^{\circ} \mathrm{T}$ at 40 kt : Variation $15^{\circ} \mathrm{E}$. If the distance from Alpha to Bravo is 300 nm , find the distance and time from the ETP to Bravo:
[a] The distance to Bravo is 136 nm and the time to Bravo is 56 min
[b] The distance to Bravo is 183 nm and the time to Bravo is 82 min
[c] The distance to Bravo is 122 nm and the time to Bravo is 39 min
[d] The distance to Bravo is 183 nm and the time to Bravo is 57 min

## Question No 5

Find the trip fuel available for a charter flight if the usable fuel on board at start-up is 140 gal .
[a] 104 gal
[b] $\quad 109 \mathrm{gal}$
[c] $\quad 120 \mathrm{gal}$
[d] 123 gal

## Question No 6

Find the distance to the PNR for a flight that has 120 gallons on board at take-off if the FPT is $290^{\circ} \mathrm{M}$, the forecast wind is $360^{\circ}$ at 40 kt and the variation is $10^{\circ} \mathrm{E}$.
[a] 408 nm
[b] 403 nm
[c] 375 nm
[d] 312 nm

## Question No 7

FPT Alpha to Bravo is $220^{\circ} \mathrm{M}$ and distance is 180 nm . If the wind is from $220^{\circ} \mathrm{M}$ at 15 kt ..
What is the distance and time from the asymmetric ETP back to Alpha?
[a] The distance back to Alpha is 78 nm and the time back to Alpha is 50 minutes
[b] The distance back to Alpha is 102 nm and the time back to Alpha is 64 minutes
[c] The distance back to Alpha is 78 nm and the time back to Alpha is 38 minutes
[d] The distance back to Alpha is 102 nm and the time back to Alpha is 49 minutes

## Question No 8

During a charter flight from Alpha to Bravo, FPT $060^{\circ} \mathrm{M}$. You overfly an on-track NDB 103 nm from Alpha. You recalculate the fuel available as 95 gallons total usable fuel. The wind has been from $070^{\circ} \mathrm{T}$ at 10 knots. The variation is $10^{\circ} \mathrm{E}$. The TAF for Bravo has no operational requirements for your planned arrival and the TAF for Alpha has a TEMPO requirement all day. The distance from Alpha to the PNR is closest to:
[a] 282 nm
[b] 275 nm
[c] 260 nm
[d] 242 nm

## Question No 9

If the headwind component increases on the flight planned track
[a] Both the PNR and the ETP will move further from the departure aerodrome
[b] Both the PNR and the ETP will move closer to the departure aerodrome
[c] The PNR will move closer to and the ETP will move further from the departure aerodrome
[d] The PNR will move further from and the ETP will move closer to the departure aerodrome

## Question No 10

You calculated the distance to the ETP and PNR during flight planning using a forecast tailwind of 30 knots. During cruise you discover that the actual tailwind is only 10 knots. How will this affect the actual position of the ETP and PNR compared to their original flight planned positions?
[a] Both the ETP and PNR will be further from the departure aerodrome
[b] Both the ETP and PNR will be closer to the departure aerodrome
[c] The ETP will be further from and the PNR will be closer to the departure aerodrome
[d] The ETP will be closer to and the PNR will be further from the departure aerodrome

## Question No 11

The following data relates to a charter flight.

| Total distance | 300 nm, FPT is $185^{\circ} \mathrm{M}$ |
| :--- | :--- |
| TAS in cruise | $150 \mathrm{kt}$. |
| Wind component from GAF | $200 / 15 \mathrm{kt}$ |
| Magnetic variation | $15^{\circ} \mathrm{E}$ |
| Fuel flow during cruise | 56 litres $/ \mathrm{hr}$. |
| Fixed reserve | 45 minutes at cruise rate. |
| Start-up and taxi allowance | 5 litres |
| Start-up is with minimum fuel required. |  |
| mine the time to the ETP and the distance to the PNR: |  |

[a] The time to the ETP is 73 min . and the distance to the PNR is 165 nm
[b] The time to the ETP is 45 min . and the distance to the PNR is 130 nm
[c] The time to the ETP is 70 min . and the distance to the PNR is 150 nm
[d] The time to the ETP is 140 min . and the distance to the PNR is 51 nm

## Question No 12

For this question, use the Echo data not the data given at the beginning of this exercise.
An Echo aircraft is to conduct a charter flight from Alpha to Bravo.
Distance from Alpha to Bravo 500 nm
Ground speed during cruise 170 kt
Cruise power 65\%
TAF for Alpha has TEMPO conditions all day.
TAF for Bravo has INTER conditions all day.
Calculate holding at 20 gallons per hour.
Usable fuel at start-up
145 gallons
Ignore any climbs and descents.
The safe endurance that should be used to calculate the position of the PNR is closest to:
[a] 288 min
[b] $\quad 208 \mathrm{~min}$
[c] $\quad 176 \mathrm{~min}$
[d] $\quad 150 \mathrm{~min}$

## ANOTHER EXAMPLE OF PNR/ETP CALCULATIONS

You are planning a charter flight in the aircraft whose details are given below.

TAS 180kt
Holding at rate 30 litres per hour
Variable reserve $10 \%$ of trip fuel
Details of the planned flight
Flight Planned Track $040^{\circ} \mathrm{M}$
Magnetic variation $10^{\circ} \mathrm{E}$
Holding required at A 60 minutes

Cruise 50 litres per hour
Fixed reserve 45 minutes at cruise rate
Taxi allowance 5 litres

Distance A to B 244 nm
GPTW wind 36030KT
Holding required at B 30 minutes
Fuel on board at start-up 190 litres

## Find

Distance from A to the PNR
Distance from the ETP to B
[Worked answer on opposite page]

## ANSWER TO ANOTHER EXAMPLE OF PNR/ETP CALCULATIONS

The only difference in this presentation is that you are not given the wind as a headwind or tailwind component, you have to work the ground speeds out for yourself from the data given. The wind from a GPWT chart is always in degrees true. So you need to apply the 10E variation. The wind is from $000^{\circ} \mathrm{T}\left(350^{\circ} \mathrm{M}\right)$ at 30 kt and the flight planned track is $040^{\circ} \mathrm{M}$. Find the ground speeds out and back from your flight computer.


Note that when you are calculating a PNR, the destination aerodrome (B), has nothing to do with it. As far as a PNR is concerned, the departure aerodrome is also your destination. In this case, you would have to allow for holding at A when you return from the PNR.

Trip fuel available for the PNR calculation
(Total fuel on board - fixed reserve - taxi - holding on return to A ) $\div 1.1$

$$
(190-37.5-5-30) \div 1.1=106.8 \text { litres }
$$

Safe endurance at 50 litres per hour

$$
106.8 \div 50 \times 60
$$

Time to PNR

Distance to PNR

Distance to ETP from A = Total distance x GS home $\div$ sum of the GSs.
$=244 \mathrm{~nm} \times 198 \div 357=135.3$
$=135 \mathrm{~nm}$.
So distance from the ETP to B = 244-135
$=109 \mathrm{~nm}$.

## ANSWERS TO EXERCISES AND TESTS TOPIC 4

## ANSWERS TO EXERCISE 4.1

No 1
Entry argument for Max rate climb on Page 14 of the supplement is density height, so find the density height.


Enter the table on Page 14 of the supplement at 5000 density height and 2950 kg

Max Rate of climb $=1500 \mathrm{ft} / \mathrm{min}$.

## No 2

Use the Density Height as the entry argument for Max rate climb table on Page 14 of the supplement.


Enter at Density Height 5000 and 2500 kg.

## Max Rate of Climb $=2100 \mathrm{ft} / \mathrm{min}$

## No 3

Use the Density Height as the entry argument for Max rate climb table on Page 14 of the supplement.


Enter at Density Height 2500 by interpolating between zero and 5000 figures. And between 2950 and 2500 kg for weight.
$[1600+1500+2250+2100] \div 4=1862.5$
Max Rate of Climb $=\mathbf{1 8 6 2 . 5} \mathbf{f t} / \mathrm{min}$

## ANSWERS TO EXERCISE 4.2

No 1
To find the time to climb you will need to know the average rate of climb and the height you climb through.


Since it is an ISA +20 day, you can add $20 \times 120=2400$ ft on to all pressure heights to obtain a density height.
If no QNH is given, you are quite justified in assuming 1013 hPa . i.e. call all heights pressure heights.

The average rate of climb is found half way between 2400 and 7400 ft . So use the 5000 ft figures for the average.

Enter at 5000 ft for rate of climb of $1500 \mathrm{ft} / \mathrm{min}$ and TAS of 109 kt .

You will climb through 5000 ft at an average rate of 1500 $\mathrm{ft} / \mathrm{min}$ so time to climb is $5000 \div 1500=\mathbf{3 . 3} \mathbf{~ m i n}$

Distance to climb is 3.3 min at an average TAS of 109 $\mathrm{kt}=6 \mathrm{~nm}$.

Fuel used in climb is 3.3 min at $100 \%$ power. [See Page 16 of the supplement], $100 \%$ power gives a fuel flow of 63.4 gph . So fuel used is $\mathbf{3 . 5} \mathbf{~ g a l}$

## No 2

Interpolate for weight between 2950 and 2500 kg Half way between Sea Level and 10000 ft in ISA conditions is 5000 ft . Average rate of climb is $[1500+2100] \div 2=1800$ $\mathrm{ft} / \mathrm{min}$. So time to climb is 10000 ft at $1800 \mathrm{ft} / \mathrm{min}=5.5 \mathrm{~min}$

Average TAS is $[109+99] \div 2=104 \mathrm{kt}$ and headwind is 25 kt giving a ground speed of 79 kt . So distance to climb is 5.5 min at $79 \mathrm{kt}=\mathbf{7 . 2 4} \mathbf{~ n m}$
Fuel used is 5.5 min at $63.4 \mathrm{gph}=\mathbf{5 . 8} \mathbf{~ g a l}$

No 3
Find the density height at Newman on this day.


Interpolate between zero and 5000 ft on single engine climb table on Page 14 of the supplement.

Rate of climb at $2500 \mathrm{~kg}=[525+450] \div 2=487.5 \mathrm{ft} / \mathrm{min} \mid$ No 5
and TAS $=[97+103] \div 2=100 \mathrm{kt}$
Time to climb from 50 ft AGL to 500 ft AGL i.e. 450 ft is $450 \div 487.5=.92 \mathrm{~min}$

Distance to climb is .92 min at 100 kt [ no wind]
$=1.53 \mathrm{~nm}$

## ANSWERS TO EXERCISE 4.3

## No 1

To obtain the rate of climb from Page 14 of the supplement, find the density height.

| 2000 |  |  |
| :---: | :---: | :---: |
| Altitude | Pressure Height |  |
| QNH 1000 | 2390 | 4190 |
| $+10$ |  | Density Height |
| ISA Temperature | +15 |  |
| +25 | ISA Deviation |  |
| OAT | [+1800] |  |

Enter at 5000 ft and 2500 kg to obtain a rate of climb of $2100 \mathrm{ft} / \mathrm{min}$ and a TAS of 99 kt .

Climb gradient $=2100 \div 99=21.21 \%$ [2 engines]
Using the single engine chart $=4.37 \%$

## No 2

At 5000 pressure height, the ISA temperature is $+5^{\circ} \mathrm{C}$. Since the temperature is given as $+25^{\circ} \mathrm{C}$, it is an ISA +20 day. Density height $=7400 \mathrm{ft}$. So enter Maximum Rate of Climb chart by interpolating between 5000 and 10000 ft and 2950 and 2500 kg .

Rate of climb $=1737.5 \mathrm{ft} / \mathrm{min}$ and $\mathrm{TAS}=108.25 \mathrm{kt}$
Climb gradient $=1737.5 \div 108.25=16.05 \%[2$ engines $]$
On one engine from single engine chart $=\mathbf{2 . 4 9 \%}$

## No 3

A QNH of 1033 and a temperature of $+5^{\circ} \mathrm{C}$ at sea level will produce a negative density height. Since the chart does not list negative values, you must use the zero figures. For 2000 kg and zero density height, rate of climb=2950 $\mathrm{ft} / \mathrm{min}$ and TAS $=82 \mathrm{kt}$
Climb gradient $=2950 \div 82=35.9 \%$ [ 2 engines]
From max climb table $=\mathbf{8 . 4 8 \%}$ on one engine

## No 4

ISA +4 , so density height is 2480 ft . Interpolate between zero and 5000 ft and 2000 and 2500 kg
Rate of climb $=2525 \mathrm{ft} / \mathrm{min}$ and $\mathrm{Tas}=90.25 \mathrm{kt}$
Climb gradient two engines $=2525 \div 90.25=\mathbf{2 7 . 9 7 \%}$
On 1 engine $=\mathbf{6 . 2 8 \%}$

Find the density height.


Interpolate between zero and 5000 for density height and between 2500 and 2950 kg .
Rate of $\mathrm{climb}=1862.5 \mathrm{ft} / \mathrm{min}$ and $\mathrm{TAS}=100.25 \mathrm{kt}$
Gradient $=1862.5 \div 100.25=\mathbf{1 8 . 5 8} \%$ [2 engines]
From single engine climb table $=\mathbf{3 . 4 9 \%}$ [1 engine]

## ANSWERS TO EXERCISE 4.4

## No 1

From the Supplement Page 15.
Climb distance $=21.5 \mathrm{~nm}$
Climb time $=8.5 \mathrm{~min}$
Climb fuel $=6 \mathrm{gal}$

## No 2

$+15^{\circ} \mathrm{C}$ at 5000 ft is ISA +10
from TAS table on Page 16 of the supplement. 5000 ft ISA $\quad 2500 \mathrm{~kg} \mathrm{75} \mathrm{\%}$ power $=192 \mathrm{kt}$ 5000 ft ISA $+202500 \mathrm{~kg} 75 \%$ power= 195 kt

So 5000 ft ISA +10 at $2500 \mathrm{~kg} 75 \%$ power $=\mathbf{1 9 3 . 5} \mathbf{k t}$.

The answers to exercises 4.5 to 4.18 have been rounded to one decimal place.

EXERCISE 4.5

| GROUND SPEED TIME |  |  |
| :--- | :--- | :--- |
| 95 | 47 | DISTANCE |
| $\mathbf{9 5 0}$ | 52 | $\mathbf{7 4}$ |
| $\mathbf{1 3 0}$ | $\mathbf{3 6}$ | 78 |
| 163 | 31 | $\mathbf{8 4}$ |
| $\mathbf{1 6 2}$ | 17 | 46 |
| 87 | $\mathbf{3 4}$ | 49 |
| 105 | 56 | $\mathbf{9 8}$ |
| $\mathbf{1 4 4}$ | 43 | 103 |

## EXERCISE 4.6

| Litres | Gallons | Kilograms |
| :--- | :--- | :--- |
| 25 | $\mathbf{7}$ | $\mathbf{1 8}$ |
| $\mathbf{2 7 7}$ | 7.3 | $\mathbf{1 9 9}$ |
| $\mathbf{2 0 0}$ | $\mathbf{5 3}$ | 144 |
| 166 | $\mathbf{4 4}$ | $\mathbf{1 2 0}$ |
| $\mathbf{3 6 9}$ | 97 | $\mathbf{2 6 4}$ |
| $\mathbf{1 2 2}$ | $\mathbf{3 2}$ | 88 |
|  |  |  |
|  |  |  |

EXERCISE 4.7

| RATE | 35 | $\mathbf{1 1 . 4}$ | 11 | $\mathbf{2 3}$ | 23 |
| :--- | :--- | :--- | :--- | :---: | :--- |
| QUANTITY | 120 | 55 | $\mathbf{3 2}$ | 65 | $\mathbf{3 6}$ |
| TIME | $\mathbf{2 0 6}$ | 290 | 175 | 170 | 93 |

EXERCISE 4.8

| FUEL REQUIRED <br> AT START-UP |  | Trip fuel |  |
| :--- | :--- | :--- | :---: |
| gallons | litres | gallons | litres |
| 32.5 | 123.5 | 20.5 | 77.9 |
| 31.7 | 120.5 | 19.7 | 74.9 |
| 48.5 | 184.3 | 36.5 | 138.7 |
| 55.5 | 210.9 | 43.5 | 165.3 |
| 25.7 | 97.7 | 13.7 | 52.1 |

EXERCISE 4.9

| FUEL REQUIRED <br> AT START-UP |  | Trip fuel |  |
| :--- | :--- | :--- | :---: |
| gallons | litres | gallons | litres |
| 43.8 | 168.5 | 31.6 | 120.2 |
| 48.2 | 183.3 | 32.1 | 121.9 |
| 24.1 | 91.5 | 14.1 | 53.4 |
| 22.9 | 87 | 11 | 41.8 |
| 103.1 | 391.8 | 81.1 | 308 |

## EXERCISE 4.10

Question No 1

| Total distance | 245 nm |
| :--- | :--- |
| Expected ground speed |  |
| Estimated time interval | 110 kt |
|  | 133.6 min |
| Trip fuel at 44 Lph | 98 L |
| Fixed reserve | 22 L |
| Start-up/taxi | 6 L |
| Alternate [28 min @ 44 Lph] | 20.5 L |
| Holding |  |
|  |  |
| Fuel required at start-up | $\mathbf{1 4 6 . 5} \mathbf{~ L}$ |
|  |  |
|  |  |
| Question No 2 | 126 nm |
|  | 155 kt |
| Total distance | 48.8 min |
| Expected ground speed |  |
| Estimated time interval | $35.8 . \mathrm{L}$ |
|  | 22 L |
| Trip fuel at 44 Lph | 6 L |
| Fixed reserve | none |
| Start-up/taxi | 25 L |
| Alternate [@ 44 Lph] | $\mathbf{8 8 . 8} \mathbf{~ L}$ |
| Holding |  |


| Question No 3 |  |
| :--- | :--- |
|  |  |
| Total distance | 89 nm |
| Expected ground speed | 130 kt |
| Estimated time interval | 41.1 min |
|  |  |
| Trip fuel at 44 Lph | 30.1 L |
| Fixed reserve | 22 L |
| Start-up/taxi | 6 L |
| Alternate [42 min @ 44 Lph] | 30.8 |
| Holding | none |
| Fuel required at start-up | $\mathbf{8 8 . 9} \mathbf{~ L}$ |

## Question No 4

| Total distance | 223 nm |
| :--- | :--- |
| Expected ground speed | 120 kt |
| Estimated time interval | 111.5 min |
|  |  |
| Trip fuel at 44 Lph | 81.8 L |
| Fixed reserve | 22 L |
| Start-up/taxi | 6 L |
| Alternate [@44 Lph] | none |
| Holding | 12.5 |
|  |  |
| Fuel required at start-up | $\mathbf{1 2 2 . 3} \mathbf{L}$ |

## PROGRESS TEST TOPIC 4

## Question No 1

[c] To convert litres to kilograms, multiply by the specific gravity. The specific gravity of AVGAS is . 72 $150 \times .72=108 \mathrm{~kg}$

## Question No 2

Total distance
180 nm
[b] Ground speed
130 kt
Time interval
Trip fuel @ 40 Lph
Fixed res 30 min @ 24 Lph
Start-up/taxi allowance
Fuel required at start-up
83.1 min
55.4 L

12 L
10 L
77.4 L

## Question No 3

[c] 2 hr 12 min is 132 min
132 min @ 12.5 GPH
27.5 gal

Start-up/taxi
2 gal
Fuel used so far
29.5 gal
29.5 gal x 3.8

## Question No 4

[a] Find the estimated time interval

| Total distance | 333 nm |
| :--- | :--- |
| Ground speed | 124 kt |
| Time interval | 161.1 min |
| Trip fuel @ 40 Lph | 107.4 L |
| Fixed reserve | 20 L |
| Start-up/taxi | 5 L |
| Fuel required at start-up | $132,4 . \mathrm{L}$ |

## Question No 5

[c] The reserves are already accounted for, so you can burn all of the 144 L .
144 L@33Lph
261.8 min
261.8 min @ 127 kt
554.1 nm

## Question No 6

| Total distance | 220 nm |
| :--- | :--- |
| Ground speed | 135 kt |
| Estimated time interval | 97.8 min |
| Trip fuel @ 9 GPH | 14.7 gal |
| Fixed reserve | 5 gal |
| Start-up/taxi | 1 gal |
| Fuel required at start-up | 20.7 gal |

## Question No 7

[c] No mention was made of a start-up/taxi allowance so ignore it. Find the total endurance at the beginning of the flight
Total endurance [205 L @ 43 Lph] 286 min From 0425 to 0630 UTC is 125 min Endurance at 0630 [286-125] $=161 \mathrm{~min}$

## Question No 8

[a] 2 hr 35 min is 155 min . In 155 min 87 L was used. Fuel consumption was 33.6 Lph

## Question No 9

[c] Find the trip fuel available
Total fuel at start-up 115 L

Fixed res of 30 min @ 28 Lph 14 L
Start-up/taxi allowance 5L
Trip fuel available 96 L
Cruise endurance @ 28 Lph 205.7 min
Distance covered at 95 kt

## Question No 10 [c]

| Total distance | 155 nm |
| :--- | :--- |
| Ground speed | 103 kt |
| Estimated time interval | 90.3 min |
| Trip fuel @ 11.5 GPH | 17.3 gal |
| Fixed res 30 min @ 8 GPH | 4 gal |
| Start-up/taxi | none |
| Holding 30 min @ 8 GPH | 4 gal |
| Fuel required at start-up | 25.3 gal |

## Question No 11

[d]
Go to page 14 of the supplement. In the maxi mum rate of climb tables consider the figures listed under 2950 kg gross weight.

At 5000 ft the rate of climb to be expected is 1500 feet per minute.

## Question No 12

[c]


## EXERCISE 4.11

Trip fuel FUEL AT START-UP

| $80 \mathrm{gal} \times 1.1+15+3$ | $=$ | 106 gal |
| :--- | :--- | :--- | :--- |
| $25 \mathrm{gal} \times 1.1+15+3$ | $=$ | 45.5 gal |
| $150 \mathrm{gal} \times 1.1+15+3$ | $=$ | 183 gal |
| $95 \mathrm{gal} \times 1.1+15+3$ | $=$ | 12.5 gal |
| $107 \mathrm{gal} \times 1.1+15+3$ | $=$ | 135.7 gal |

## EXERCISE 4.12

FUEL AT
START-UP

| 1 | $[150 \mathrm{gal}-15-3] \div 1.1$ | $=$ | 120 gal |
| :--- | :--- | :--- | :--- |
| 2 | $[100 \mathrm{gal}-15-3] \div 1.1$ | $=$ | 74.5 gal |
| 3 | $[95 \mathrm{gal}-15-3] \div 1.1$ | $=$ | 70 gal |


| EXERCISE 4.13 |  |  |  |
| :---: | :---: | :---: | :---: |
|  | TRIP FUEL |  | START UP |
| 1 | 84 gal x $1.1+15+3$ | = | 110.4 gal |
|  | $228.5 \mathbf{~ k g ~ x ~} 1.1+41+8$ | $=$ | 300.4 kg |
| 2 | $200 \mathrm{~kg} \mathrm{x} 1.1+41+8$ | $=$ | 269 kg |
|  | 73.5 gal x 1.1+15+3 | = | 98.9 gal |
| 3 | [120 gal - 15-3] $\div 1.1$ | $=$ | 92.7 gal |
|  | [ $\mathbf{3 2 6 . 4} \mathbf{~ k g ~ - ~} 41-8$ ] $\div 1.1$ | $=$ | 252.1 kg |
| 4 | [ $300 \mathrm{~kg}-41-8] \div 1.1$ |  | 228.2 kg |
|  | [ 110.3 gal - 15-3] $\div 1.1$ |  | 83.9gal |
| 5 | $120 \mathrm{~kg} \mathrm{x} 1.1+41+8$ | = | 180.9 kg |
|  | 44.1 gal $\mathrm{x} 1.1+15+3$ | = | 66.5 gal |
| EXERCISE 4.14 |  |  |  |
| $155 \mathrm{~min} @ 28 \mathrm{gph}=73$ 30 min @ $17.2 \mathrm{gph}=8.6$ |  |  |  |
| Min fuel $=73 \times 1.1+15+8.6+3=\mathbf{1 0 6 . 9}$ gal |  |  |  |
| 204 min @ 28 gph = 96 60 min @ 17.2 gph = 17.2 |  |  |  |
| Min fuel $=96 \times 1.1+15+17.2+3$ = $\mathbf{1 4 0 . 8}$ gal |  |  |  |
| $97 \mathrm{~min} @ 28 \mathrm{gph}=46 \mathrm{gal} 45 \mathrm{~min} @ 17.2 \mathrm{gph}=12.9$ |  |  |  |
| Min fuel $=46 \times 1.1+15+12.9+3 \quad=8.5$ gal |  |  |  |
| 135 min @ 28 gph = 63 gal $30 \mathrm{~min} @ 17.2 \mathrm{gph}=8.6$ |  |  |  |
|  |  |  |  |
| 84 min @ 28 gph = 40 gal 60 min @ $17.2 \mathrm{gph}=17.2$ |  |  |  |
| Min fuel $=40 \times 1.1+15+17.2+3 \quad=79.2$ gal |  |  |  |

EXERCISE 4.15



ANSWERS TO EXERCISE 4.16

| ISA CONDITIONS | POWER | TAS | WIND | G/ SPEED | F/ FLOW | ANMPG | GNMPG |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $2500 \mathrm{~kg} / 10000 \mathrm{ft}$ | $65 \%$ | 185 | ----- | 185 | 28 gph | 6.61 | 6.61 |
| $2950 \mathrm{~kg} / 15000 \mathrm{ft}$ | $75 \%$ | 205 | -30 | 175 | 32.6 gph | 6.29 | 5.37 |
| $2725 \mathrm{~kg} / 12500 \mathrm{ft}$ | $55 \%$ | 170.75 | +25 | 195.75 | 23.6 gph | 7.23 | 8.29 |
| $2500 \mathrm{~kg} / 7500 \mathrm{ft}$ | $65 \%$ | 181.5 | -10 | 171.5 | 28 gph | 6.48 | 6.12 |

## ANSWERS TO EXERCISE 4.17

## No 1

Find the TAS. 10000 ISA $2500 \mathrm{~kg} 65 \%=185 \mathrm{kt}$ [nil wind]
Trip fuel $\quad=$ Distance $\times$ Fuel Flow $\div$ Ground Speed
$=285 \times 28 \div 185=43.1 \mathrm{gal}$
Min fuel $=43.1 \times 1.1+15+3=\mathbf{6 5 . 4} \mathbf{g a l}$
No 2
Find the TAS 15000 ISA $+202725 \mathrm{~kg} 55 \%=175.5 \mathrm{kt}$
Ground Speed $=175.5-25=150.5 \mathrm{kt}$
Trip fuel $\quad=$ Distance $\times$ Fuel Flow $\div$ Ground Speed

$$
=358 \times 23.6 \div 150.5=56.1 \mathrm{gal}
$$

Min fuel $=56.1 \times 1.1+15+3=79.7$ gal
No 3
Find the TAS 5000 ISA - $1075 \% 2950 \mathrm{~kg}=187$
Ground Speed $=187+15=202 \mathrm{kt}$
Trip fuel $\quad=$ Distance $\times$ Fuel Flow $\div$ Ground Speed
$=547 \times 32.6 \div 202=88.3 \mathrm{gal}$
Min fuel $=88.3 \times 1.1+15+3=\mathbf{1 1 5 . 1}$ gal
No 4
17500 [ISA + 10 day] 2250 kg
Investigate best ground nautical miles per gallon.
POWER TAS WIND G/S F/FLOW MPG
$\begin{array}{lllllll}55 \% & 182.25 & -30 & 152.25 & 23.6 & 6.45\end{array}$
$\begin{array}{llllll}45 \% & 154.87 & -30 & 124.87 & 20.4 & 6.12\end{array}$
So use $55 \%$ power for best GNMPG.
$\begin{aligned} \text { Trip fuel } & =\text { Total Distance } \div \text { GNMPG } \\ & =766 \div 6.45=118.7 \\ \text { Min fuel } & =118.7 \times 1.1+15+3=\mathbf{1 4 8 . 6} \mathbf{~ g a l}\end{aligned}$

## ANSWERS TO EXERCISE 4.18

## No 1

Find how much of the 120 gal on board at start up is available as trip fuel.

$$
\begin{array}{ll}
{[120-15-3] \div 1.1} & =92.7 \mathrm{gal} \\
\text { Less transit fuel } & =42 \mathrm{gal}
\end{array}
$$

Available for search $=50.7 \mathrm{gal}$
Burn 50.7 gal at $17.2 \mathrm{gph}=177 \mathrm{~min}$.

## No 2

Fuel required for the search $=90 \mathrm{~min}$ at 17.2 gph

$$
\text { Transit fuel } \quad=35 \mathrm{gal}
$$

$$
\text { Trip fuel required } \quad=60.8 \mathrm{gal}
$$

Min fuel required

$$
\begin{aligned}
& =25.8 \mathrm{gal} \\
& =35 \mathrm{gal} \\
& =60.8 \mathrm{gal} \\
& =60.8 \times 1.1+15+3 \\
& =\mathbf{8 4 . 9} \mathbf{~ g a l}
\end{aligned}
$$

No 3
Minimum fuel req'd for the flight $53 \times 1.1+15+3$
$=76.3 \mathrm{gal}$
Actual fuel available at start up $=100 \mathrm{gal}$
Margin fuel available for holding $=23.7 \mathrm{gal}$
This margin can be burnt at the holding rate of 17.2 gph
Maximum holding time
$=82.7 \mathrm{~min}$

## No 4

Find how much of the 144 gal is available as trip fuel Trip fuel available $=[144-15-3] \div 1.1=114.5 \mathrm{gal}$ Less transit fuel to and from the search area $=67 \mathrm{gal}$ Fuel available for holding $=47.5 \mathrm{gal}$ Burn 47.5 gal @ 17.2 gph $=\mathbf{1 6 5 . 7} \mathbf{~ m i n}$

No 5
Fuel required for the search = 2 hours @ 17.2 gph

|  | $=34.4 \mathrm{gal}$ |
| ---: | :--- |
| Plus transit fuel | $=18 \mathrm{gal}$ |
| Total trip fuel required | $=52.4 \mathrm{gal}$ |
| Min fuel req'd at start up | $=52.4 \times 1.1+15+3 \mathrm{gal}$ |
|  | $=\mathbf{7 5 . 6} \mathbf{~ g a l}$ |

## No 6

Minimum fuel req'd for the flight $=66 \times 1.1+15+3$

$$
=90.6 \mathrm{gal}
$$

Actual fuel available at start up $=102 \mathrm{gal}$
Margin fuel available for holding $=11.4 \mathrm{gal}$
Burn 11.4 gal @ 17.2 gph $=\mathbf{3 9 . 8}$ min

## No 7

Minimum fuel required to proceed to the alternate $=26+$ fixed reserve of 15 gal [no taxi fuel of course]
$=41 \mathrm{gal}$
Actual fuel available on arrival $=50 \mathrm{gal}$
Margin fuel available for holding $=9 \mathrm{gal}$
Burn 9 gal @ 17.2 gph $=31.4$ min
Latest time for diversion to the alternate

$$
\begin{aligned}
& =0412+31.4 \\
& =0443
\end{aligned}
$$

## ANSWERS TO ETP/PNR REVISION

Question No 1 Answer [d]


Trip fuel = 67 gals @ 23 gph = 174.8 mins. Time to $\mathrm{PNR}=175 \times 170 \div 315=94.3 \mathrm{mins}$. Distance to $\mathrm{PNR}=94.3 \mathrm{~min} @ 145 \mathrm{kt}=\mathbf{2 2 7 . 9} \mathbf{~ n m}$.


Question No $4 \quad$ Answer [d]

GS home 124 $\square$ GS out 194

FPT $025^{\circ} \mathrm{M}$ : Wind $175^{\circ}$ at 40 kt : TAS 160

Question No $5 \quad$ Answer [b]

Trip fuel $=[140-3-17.25] \div 1.1=\mathbf{1 0 9}$ gal.


The ETP always moves upwind from half way and the stronger the wind, the further upwind it moves. So an increase in headwind component will cause the ETP to move towards the destination end of the track, i.e. further away. The PNR is always the greatest distance out in nil wind conditions, any wind, head or tail, will move the PNR closer to base.

## Question No 10 Answer [a]

The ETP moves up wind from half way. Based on a tail wind of 30 knots, the calculated position of the ETP would therefore be closer to the departure aerodrome than half way. If the actual tailwind was less than expected the ETP would be closer to half way than the calculated position. i.e. further from the departure aerodrome. If the wind component reduced the PNR would be further away since it is always furtherest out in no wind.

Question No 11 Answer [a]
The wind is an exact headwind $\left(185^{\circ} \mathrm{M}\right)$

| $150-15=165 \longrightarrow$ 【 $150+15=135$ |  |
| :---: | :---: |
| 15 kt |  |
| 300 nm |  |
|  | $=300 \times 165 \div 300$ $=165 \mathrm{~nm}$ |
| Time to ETP | $=165 \mathrm{~nm} @ 135 \mathrm{kt}=73.3 \mathrm{mins}$. |
| Trip fuel | $\begin{aligned} & =300 \times 56 \div 135 \\ & =124.4 \text { litres. } \end{aligned}$ |
| Safe endurance | $=124.4$ litres @ $56 \mathrm{lph}=133.3 \mathrm{~min}$. |
| Time to PNR | $\begin{aligned} & =133.3 \times 165 \div 300 \\ & =73.3 \text { minutes } . \end{aligned}$ |
| Distance to PNR | $\begin{aligned} & =73.3 \text { mins } @ 135 \text { knots } \\ & =\mathbf{1 6 4 . 9} \mathbf{n m} . \end{aligned}$ |

Question No 12 Answer [b]
If you fly to the PNR and back to Alpha, you will need the 60 minutes holding when you arrive at Alpha due to the TEMPO requirement. Therefore trip fuel available for the PNR calculation is:
[Total fuel - taxi - fixed res. - 60 min holding ] $\div 1.1$
[145-3-15-20] $\div 1.1=97.3$ gallons.
Safe endurance $\quad=97.3$ gallons @ 28 gph
$=209$ minutes.

## TOPIC 5 - LOADING

## STRUCTURAL WEIGHT LIMITATIONS

Having established the minimum fuel requirements for a flight, the operator will often need to consider the maximum payload that can be carried, especially in commercial operations. One of the factors that may control the maximum payload possible is the limitations on aircraft weight imposed by the manufacturer. Because these limitations consider the stresses that can be tolerated by the aircraft structure, they are called structural limitations.

> The structural take-off weight limitation
> The structural landing weight limitation
> The zero fuel weight structural limitation

The structural take-off weight limitation is imposed to prevent excessive loads on undercarriage components during the take-off run. It considers such things as side loads imposed by cross winds and the loads imposed by rough surfaces.

The structural landing weight limitation Many light aircraft manufacturers simply publish one structural weight limitation which applies to all flight situations. For example the Cessna 172 RG usually has a maximum weight limitation of 2650 lbs [ 1203 kg ]. This is the maximum weight for take-off or landing. However some larger aircraft may have a different weight limit for landing which, because it considers the possibility of a heavier than normal landing, may be lower than the take-off weight limitation. It is imposed to prevent excessive loads on the undercarriage at touch-down and during the landing roll.

The zero fuel weight structural limitation is imposed on many larger aircraft to prevent excessive loads on the airframe during flight.

Compare the aircraft in the illustration in the figure at right with the plank below. Since each wing contributes equally to total lift in normal flight, and the total weight of the aircraft acts through the centre of gravity which is located somewhere in the aircraft's fuselage, bending loads are imposed on the aircraft structure especially at the wing roots.

This arrangement of forces is similar to the situation depicted in Fig 5.1 at right. The plank is suspended by two ropes and a heavy weight is suspended from the centre of the plank.

The heavy weight represents items such as passengers and cargo which are normally placed in the fuselage.


